

## A reformulation of the level set equation with built-in redistancing

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The level set method introduced by Osher and Sethian [1, 2] is one of the most popular numerical methods to track a moving interface. It is based on the idea to represent the interface as the zero contour of a smooth function  $\phi$ . Given a smooth velocity field  $\vec{v} \in \mathbb{R}^n$  advecting the interface  $\Sigma$ , the usual *choice* for the transport equation for  $\phi$  is the linear hyperbolic PDE

$$\partial_t \phi + \vec{v} \cdot \nabla \phi = 0. \quad (1)$$

Moreover, the initial value for  $\phi$  is frequently chosen to be (locally) the signed distance to the interface since the latter has some convenient properties (e.g., to compute the mean curvature). However, one can easily show that a solution of (1) does not preserve the signed distance property. That is why reinitialization (or redistancing) algorithms are applied to restore the signed distance property after advection [2]. In this work, we propose a reformulation of (1) based on the fundamental kinematics of interfaces [3]. The resulting nonlinear PDE preserves  $|\nabla \phi|$  at the moving interface. We show that, on the discrete level, it is sufficient to solve a linear equation for  $\phi$  in each time step.

### REFERENCES

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