Deep Learning in Scientific Computing

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MANUEL J. CASTRO\*, SIDDARTHA MISHRA†   
and DAVID PARDO^

\* Univ. of Málaga

Dept. of Mathematical Analysis, Campus de Teatinos S/N, 29081 Malaga, Spain

[mjcastro@uma.es](mailto:mjcastro@uma.es), [www.uma.es/edanya](http://www.uma.es/edanya)

† ETH Zurich

Dept. of Mathematics, Rämistrasse 101, 8092 Zurich, Switzerland

[siddhartha.mishra@sam.math.ethz.ch](mailto:siddhartha.mishra@sam.math.ethz.ch), <https://math.ethz.ch/sam/the-institute/people/siddhartha-mishra.html>

^ Univ. of the Basque Country (UPV/EHU), BCAM, and Ikerbasque

Dept. of Mathematics, Barrio Sarriena S/N, 48940 Leioa, Spain

[dzubiaur@gmail.com](mailto:dzubiaur@gmail.com), [www.mathmode.science](http://www.mathmode.science)

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ABSTRACT

Deep learning i.e., the use of deep neural networks for regression and classification, has been very successful in many different contexts in science and engineering. These include image analysis, natural language understanding, game intelligence, and protein folding. As deep neural networks are universal function approximators, it is natural to employ them as ansatz spaces for solutions of ordinary and partial differential equations, paving the way for their successful use in scientific computing. An incomplete list of examples where deep learning is used for the numerical solutions of differential equations includes the solution of high-dimensional linear and semi-linear parabolic partial differential equations and many-query problems such as those arising in uncertainty quantification (UQ), PDE constrained optimization, and (Bayesian) inverse problems.

Another interesting use of deep learning is data-driven computing, that is to combine available data with existing physical laws to more accurately predict events as diverse as the spread of pandemics, the weather forecast, the behavior of a vehicle, a structure, or a drug, among others. Deep learning algorithms can be used to solve all these problems. Moreover, they have been the best performers in the last decade, and are being massively adopted by various industries and institutions.

Previous problems can be recast as parametric partial differential equations and the use of deep neural networks in their solution is explored for elliptic and parabolic PDEs, for transport PDEs and for hyperbolic and related PDEs, and as operator learning frameworks. All the afore-mentioned methods are of the supervised learning type, i.e., the underlying deep neural networks have to be trained on data, either available from measurements or generated by numerical simulations

Another interesting application of deep learning algorithms is the so-called Physics Informed Neural Networks (PINNs) which collocate the PDE residual on training points of the approximating deep neural network. This is an interesting approach where generating training data might be very expensive. PINNs have been successfully applied to simulate a variety of forward and inverse problems for PDEs.

This minisymposium accepts contributions that employ deep learning techniques to predict the result of physical systems often governed by ordinary and/or partial differential equations and are possibly complemented with measured data. We encourage works ranging from the mathematical analysis of these methods to their industrial applications.